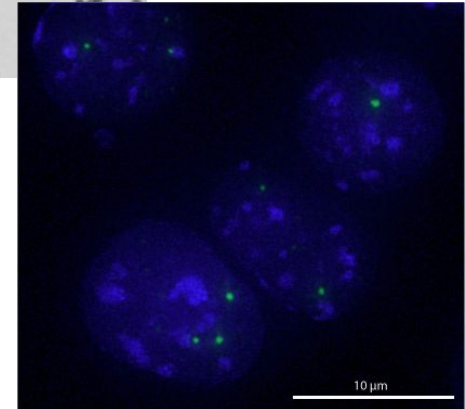
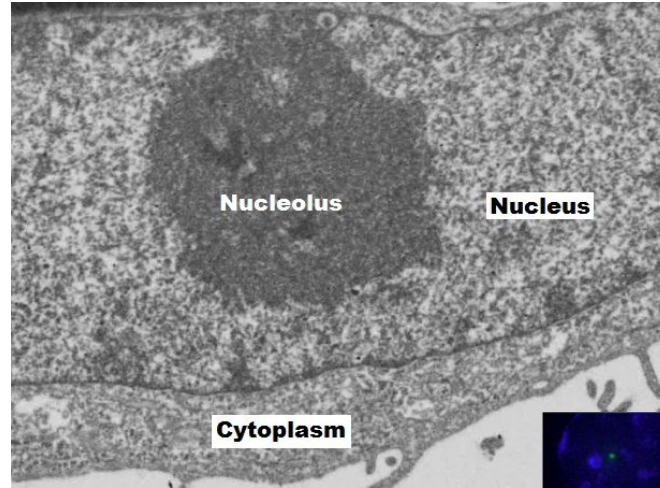
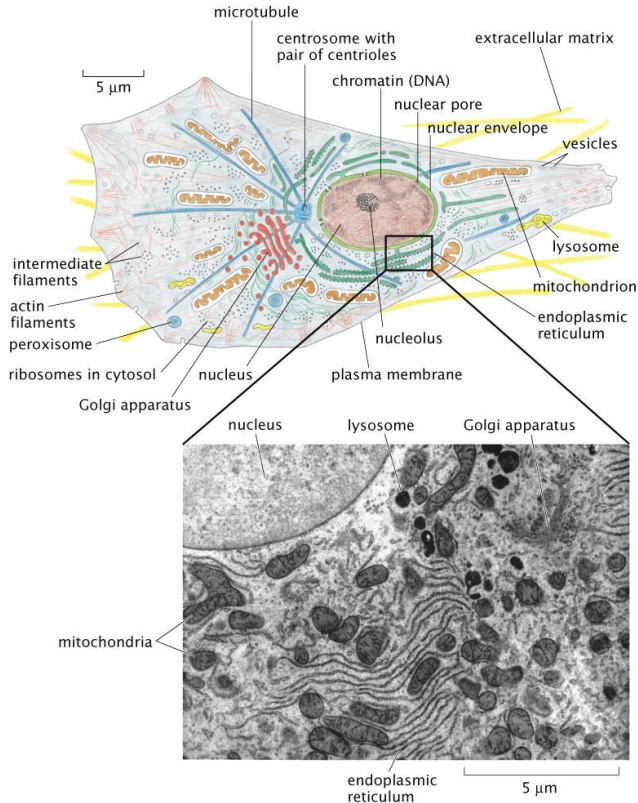


Phase transitions and membrane-less organelles in biology

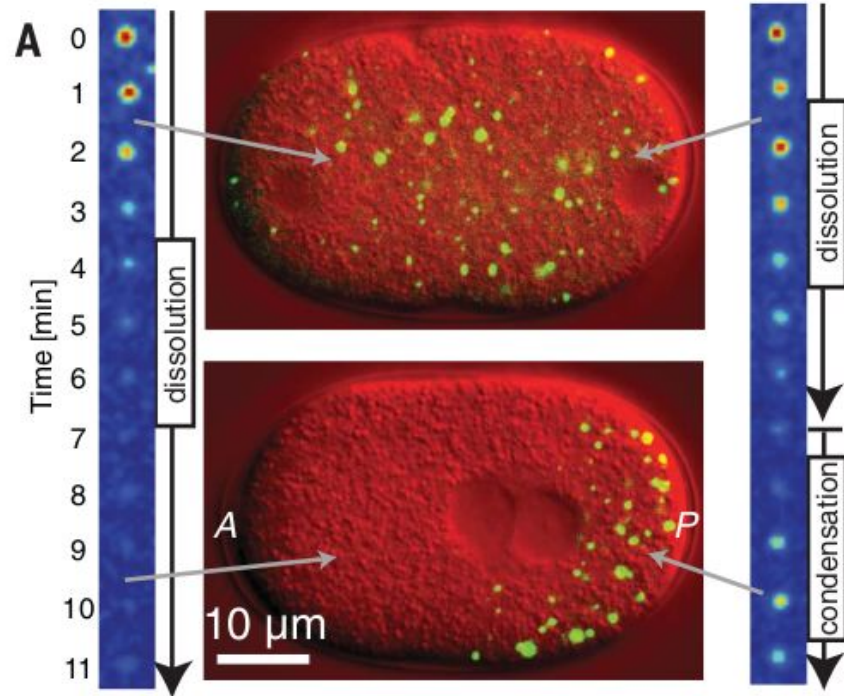
Physics of Life 1

Organelles with and without membrane enclosure

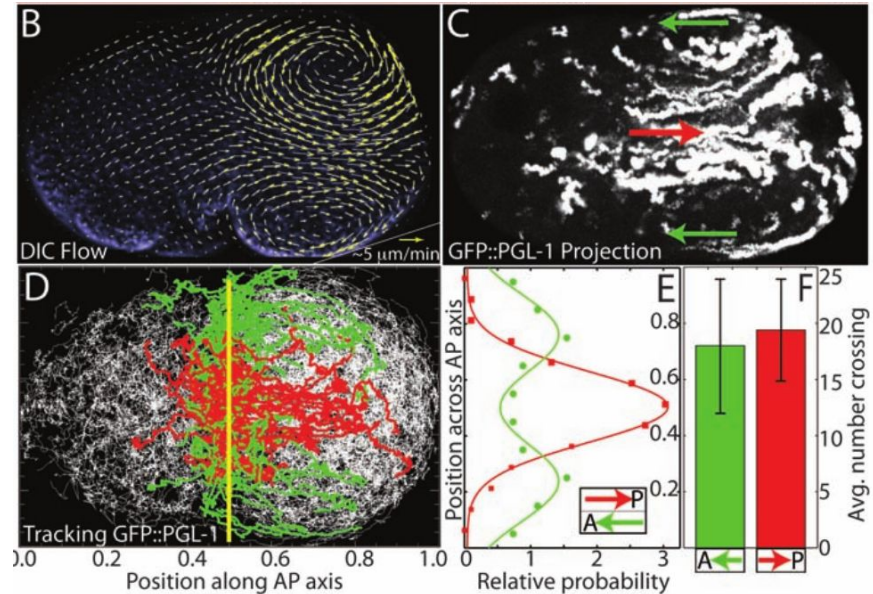


wikipedia.org

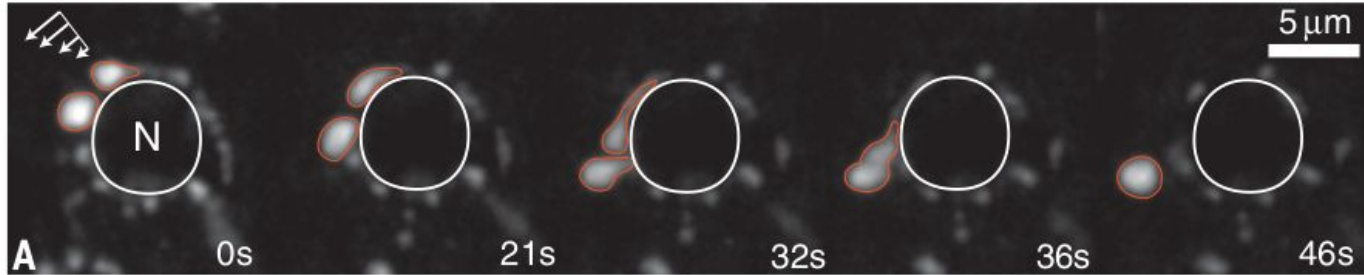
P-granules in *C. elegans* embryos



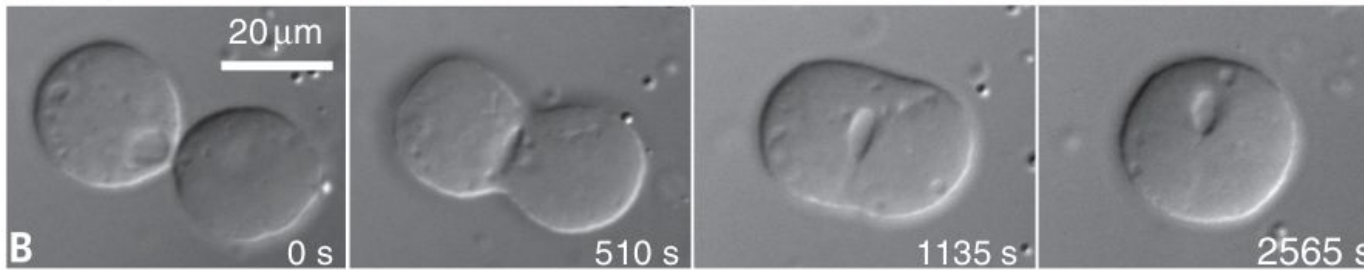
- B**
- Puncta that all end-up in the posterior cell (and ultimately the germ cells)
 - Puncta disappear and appear
 - Puncta move around, but there is no net flux



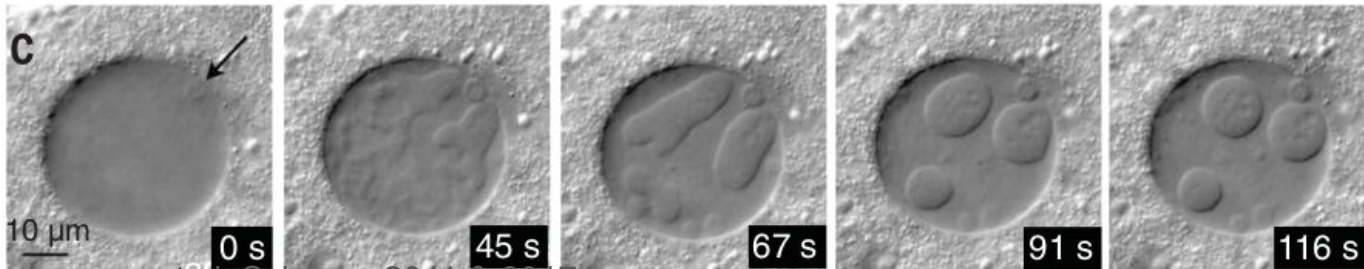
P-granules have liquid-like properties



P-granules in *C.elegans* drip and flow

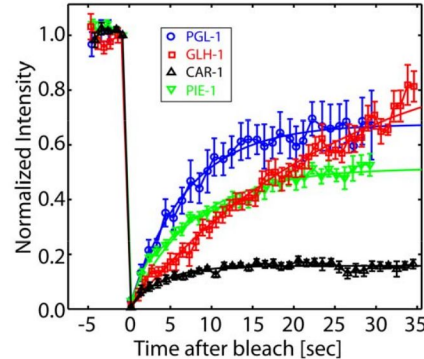
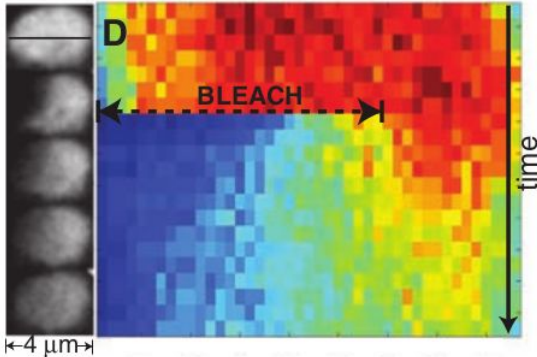
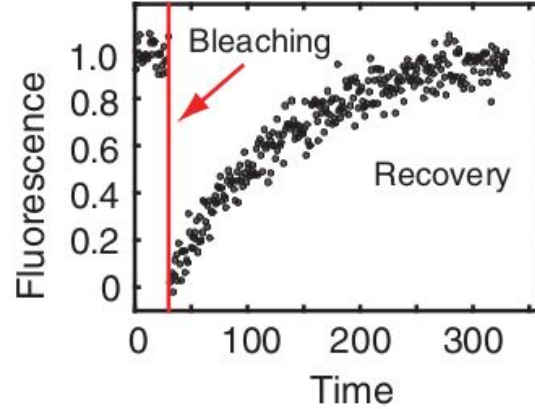
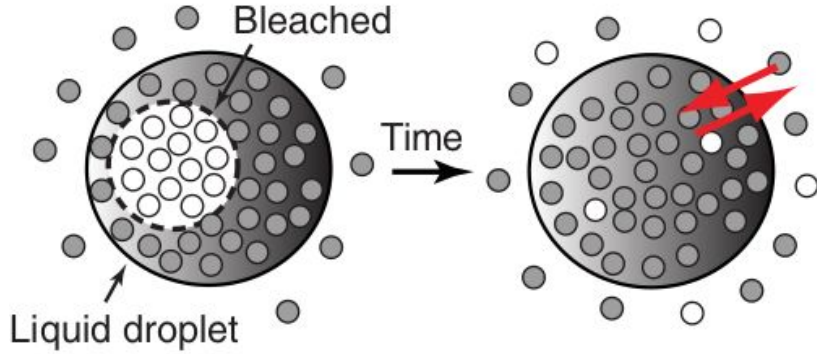


Fusion of nucleoli in *Xenopus*



Liquid-like nuclear bodies in *Drosophila* embryos

Diffusion within droplets and between cytosol and droplet



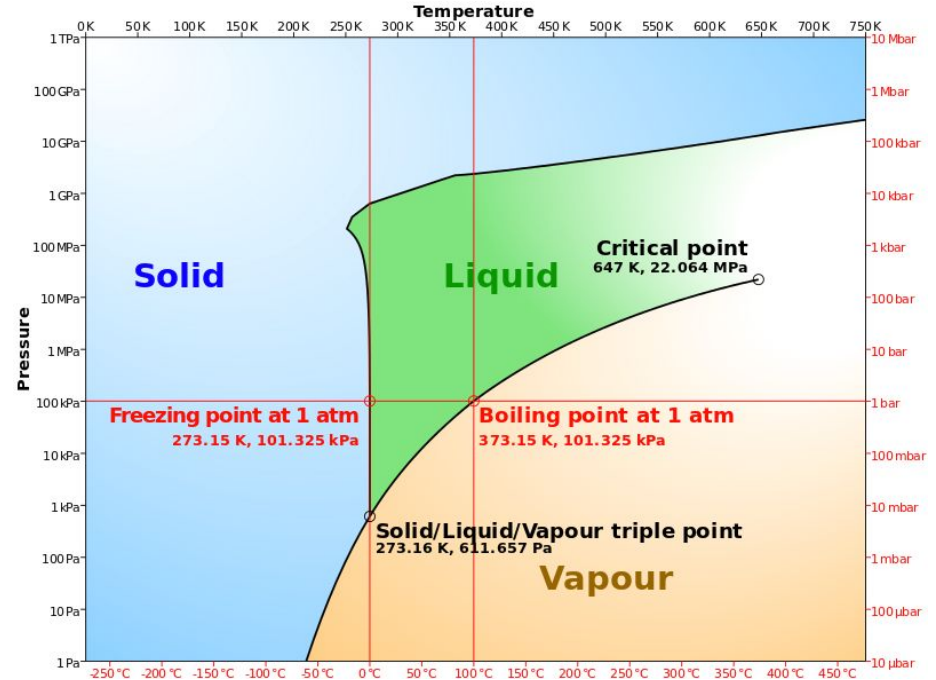
tions were made with GFP::GLH-1 embryos (movie S12). Using the length scale of these large granules, $L \sim 4 \mu\text{m}$, we obtained a diffusion coefficient on the order of $D \sim L^2/\tau \sim 1 \mu\text{m}^2/\text{s}$. By making the simplifying assump-

Hypothesis: These droplets form through phase separation

Background: <https://www.youtube.com/watch?v=AP47mlkd-h0>

Classical phases of water

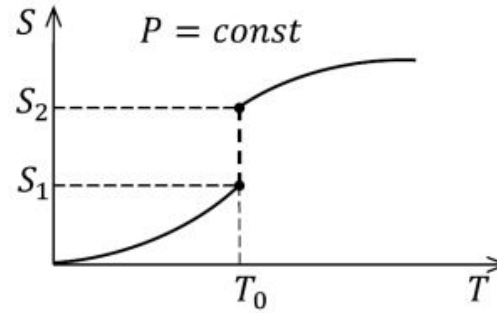
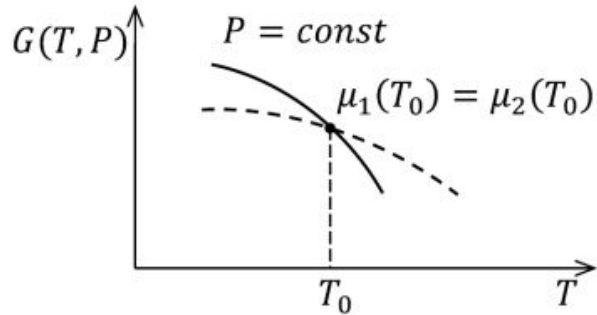
- 3 phases (many phases of ice)
- Phase diagram:
 - State of the systems as function intensive variables (T, pressure)
- Different coexistence regimes
 - Single phases
 - Phase boundaries
 - Triple points
- Critical point
 - Point where 'difference between liquid and gas' disappears



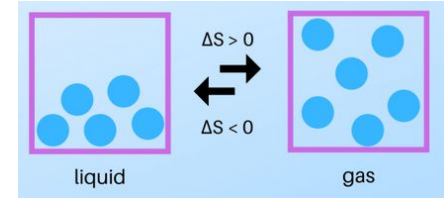
First order phase transitions

- Discontinuous first derivative of thermodynamic potential

$\frac{\partial G}{\partial T} = -S$ jumps at the boiling point.



Latent heat: $\Delta Q = T(S_2 - S_1)$

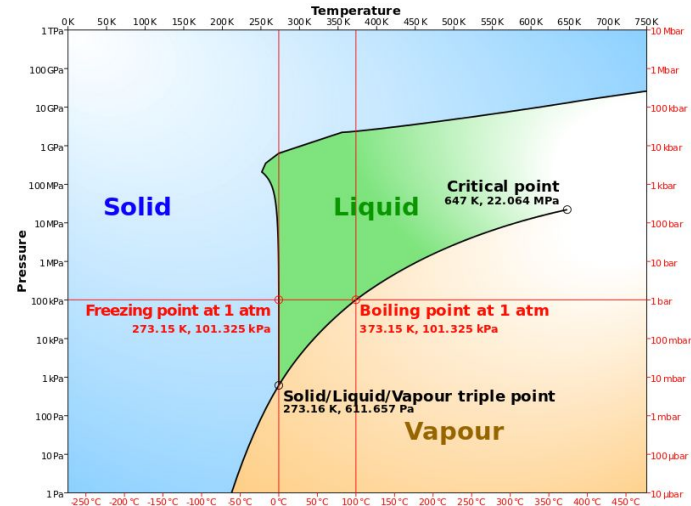


Phase coexistence

- At equilibrium, a multicomponent system minimizes the Gibbs Free energy:

$$G(T, P) = N_1 \frac{G_1}{N} + N_2 \frac{G_2}{N} = N_1 \mu_1(T, P) + N_2 \mu_2(T, P)$$

- If multiple phases co-exist, they share
 - Temperature T
 - Pressure p
 - Chemical potential of each component $\mu = \mu_1 = \mu_2$
(if chemical potential differed, one phase would disappear)
- Equal chemical potential == constrains
 - Two phase coexistence \rightarrow line in phase diagram
 - Tree phase coexistence \rightarrow point



Gibbs' phase rule: the number of coexisting phases

Consider a system with c different molecular species and two intensive control parameters (e.g. temperature and pressure).

- If p co-exist, all c chemical potentials have to be equal in all phases
→ $c(p-1)$ constraints
- In each phase, the concentrations of each component is free to adjust
→ $(c-1)p$ free parameters

In a 2-d phase diagram, the remaining degrees of freedom with p phases is:

$$f = 2 + (c-1)p - c(p-1) = 2 + c - p$$

(in biology, we can have as many phases as we want)

What could drive phase transitions biology cases?

- Changing overall concentration of constituents
- Changing interaction strength (through modifications, changing abundance of 'sticky molecules' that mediate interactions)
- These are changes in intensive parameters